

GUJARAT TECHNOLOGICAL UNIVERSITY**B.E. Sem-Vth Examination December 2010****Subject code: 151002****Subject Name: Engineering Electromagnetics****Date: 15 /12 /2010****Time: 03.00 pm - 05.30 pm****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1 (a)** Answer the following in brief **08**
- (i) 'The divergence of the curl of a vector is zero'-Justify the statement with one example.
 - (ii) Find the $\mathbf{a}_y \cdot \mathbf{a}_\phi$ and $\mathbf{a}_x \cdot \mathbf{a}_\theta$
 - (iii) Given 60 μC point charge located at the origin, find the total electric flux passing through that portion of the sphere $r=26$ cm bounded by $0 < \theta < \pi/2$ and $0 < \phi < \pi/2$.
 - (iv) For a coaxial cable find the electric field density inside the inner core, in between inner and outer core and outside the cable.
- (b)** Answer the following **06**
- (i) What is Gradient? with help of gradient prove that $\nabla = - \nabla V$
 - (ii) Find the volume charge density that is associated with $\mathbf{D} = \rho z^2 \sin^2 \phi \mathbf{a}_\rho + \rho z^2 \sin \phi \cos \phi \mathbf{a}_\phi + \rho^2 z \sin^2 \phi \mathbf{a}_z$ c/m²
- Q.2 (a)** Derive the electric field intensity and electric field density due to an infinite and uniform line charge density. **07**
- (b)** In the space, a line charge $\rho_L=80$ nC/m lies along the entire Z-axis, while point charge of 100 nC each are located at (1,0,0) and (0,1,0). Find the potential difference V_{PQ} given P (2,1,0) and Q (3,2,5). **07**
- OR**
- (b)** Given the flux density $\mathbf{D} = (2\cos\theta/r^3) \mathbf{a}_r + (\sin\theta/r^3) \mathbf{a}_\theta$ c/m², evaluate both sides of the divergence theorem for the region defined by $1 < r < 2$, $0 < \theta < \pi/2$, $0 < \phi < \pi/2$ **07**
- Q.3 (a)** Describe the boundary condition between free space and conductor. What is an importance of boundary condition? **07**
- (b)** Write Maxwell's equations in point form and explain physical significance of equations. **07**
- OR**
- Q.3 (a)** Derive Poisson's and Laplace's equations and states their applications. **07**
- (b)** Write Maxwell's equations in integral form and explain their physical significance. **07**
- Q.4 (a)** State and explain Ampere's circuital law. Find the magnetic field intensity due to long straight conductor using Ampere's circuital law. **07**
- (b)** A charge of 10 nC is moving with a velocity of $10^7(-0.5 \mathbf{a}_x + \mathbf{a}_y - 0.71 \mathbf{a}_z)$ m/s. **07**
- Determine the force exerted on the test charge when
- (i) a magnetic induction $\mathbf{B} = (\mathbf{a}_x + 2\mathbf{a}_y + 3 \mathbf{a}_z)$ mWb/m² is applied
 - (ii) an electric field $\mathbf{E} = (3\mathbf{a}_x + 2\mathbf{a}_y + \mathbf{a}_z)$ kV/m is applied.
 - (iii) When $\mathbf{B}$ and $\mathbf{E}$ given above are applied simultaneously.

OR

- Q.4 (a)** What is curl? With help of curl meter explain the physical interpretation of curl and state its applications. **07**
- (b)** A filamentary current of 10 A is directed in from infinity to the origin on the positive x axis, and then back to infinity along the positive y axis. Use the Biot-Savart law to find H at P (0,0,1) **07**

- Q.5 (a)** Define and explain the following terms: **07**
- (i) Magnetization (ii) Polarization
(iii) Skin effect and (iv) Standing wave ratio
- (b)** Write short note on: **07**
- (i) Wave motion in free space
(ii) Magnetic boundary condition

OR

- Q.5 (a)** Define and explain the following terms: **07**
- (i) Poynting Vector (ii) The scalar and Vector magnetic potential
(iii) Hall effect (iv) Retarded Potential
- (b)** (i) Transform the $5a_x$ vector to spherical coordinate at $A(x = 2, y = 3, z = -1)$. **07**
- (ii) Given $V = (10/r^2) \sin\theta \cos\phi$, Find the electric flux density at $(2, \pi/2, 0)$
