

GUJARAT TECHNOLOGICAL UNIVERSITY**B.E. Sem-Vth Examination December 2010****Subject code: 151601****Subject Name: Computer Oriented Statistical Methods****Date: 13 /12 /2010****Time: 03.00 pm - 05.30 pm****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q-1** (a) Use three iterations of Newton Raphson Method to solve the non-linear equations, $x^2 - y^2 + 7 = 0, x - xy + 9 = 0$. Take $(x_0, y_0) = (3.5, 4.5)$ as the initial approximation. **06**
- (b) (i) Discuss the pitfalls in computing using normalized floating – point numbers. **03**
(ii) Find all roots of the equation $x^3 - 2x^2 - 5x + 6 = 0$ using Graeffe's method squaring thrice. **05**

- Q-2** (a) Obtain cubic spline for every subinterval from the following data **06**
 $x :$ 0 1 2 3
 $f(x) :$ 1 2 33 244
Hence an estimate $f(2.5)$
- (b) (i) The population of the town in decennial census was as given below estimate the population for the year 1895 **06**
Year : 1891 1901 1911 1921 1931
Population: 46 66 81 93 101
(In thousand)
- (ii) Write an algorithm for the successive approximation method to find root of non-linear equation. **02**

OR

- (b) (i) If P is the pull required to lift a load W by means of pulley block, find a linear law of the form $P = mW + c$ connecting P and W using following data: **06**
 $P :$ 12 15 21 2
 $W :$ 50 70 100 120
Where P and W are taken in kg-wt. compute P when $W = 150$ kg.
- (ii) Write an algorithm for Lagrange's interpolation method to interpolate a value of dependent variable for given value of independent variable. **02**
- Q-3** (a) The distance (s) covered by a car in a given time (t) is given below **06**
Time(Minutes) : 10 12 16 17 22
Distance(Km.) : 12 15 20 22 32
Find the speed of car at time $t = 14$ minutes.
- (b) (i) Evaluate : $\int_1^5 \log_{10} x dx$, taking 8 subintervals, correct to four decimal places by Trapezoidal rule. **06**
- (ii) Write an algorithm for Simpson's three-eighth rule to integrate a tabulated function. **02**

OR

- Q-3** (a) The following data gives pressure and volume of superheated steam **06**
 $V :$ 2 4 6 8 10
 $P :$ 105 42.7 25.3 16.7 13
Find the rate of change of pressure w.r.t. volume when $V = 8$

- (b) (i) Following table shows speed in m/s and time in second of a car 06
 t : 0 12 24 36 48 60 72 84 96 108 120
 v : 0 3.60 10.08 18.90 21.60 18.54 10.26 5.40 4.50 5.40 9.00
 Using Simpson's one-third rule find the distance travelled by the car in 120 second
- (ii) Evaluate $\int_2^4 (x^2 + 2x) dx$ using Gauss's quadrature formula with $n=3$. 02
- Q-4** (a) Use three iterations of Jacobi's method to solve the system of equations 06
 $20x + y - 2z - 17 = 0, 2x - 3y + 20z - 25 = 0, 3x + 20y - z + 18 = 0$
- (b) (i) Given that $\frac{dy}{dx} = x + y^2, y(0) = 1$. Using Runge-kutta method find approximate value of $y(0.2)$, take step size 0.1 06
- (ii) Write an algorithm for Euler's method to solve ODE $\frac{dy}{dx} = f(x, y)$ 02
- OR**
- Q-4** (a) Use Gauss elimination method to solve the equations: 06
 $2x + y + z = 10, 3x + 2y + 3z = 18, x + 4y + 9z = 16$. also write pseudo code for this method.
- (b) (i) Given that $2\frac{dy}{dx} = y^2 + x^2 y^2, y(0) = 1, y(0.1) = 1.06, y(0.2) = 1.12, y(0.3) = 1.21$ 06
 evaluate $y(0.4)$ by Milnes predictor-corrector method.
- (ii) Write a pseudo code for Gauss-seidel method to solve linear system of equations 02
- Q-5** (a) The following table gives the profits(in thousand Rs.) of two companies X and Y for last 10 years. Which of two companies has greater consistency in profits: 07
 Year : 1979 1980 1981 1982 1983 1984 1985 1986 1987 1988
 Profits(X): 700 625 725 625 650 700 650 700 600 650
 Profits(Y): 550 600 575 550 650 600 550 525 625 600.
- (b) Find the first four central moments of the following distribution and comment on the nature of the distribution: 07
 Class-limits: 100-104.9 105-109.9 110-114.9 115-119.9 120-124.9
 Frequency : 7 13 25 25 30
- OR**
- Q-5** (a) Calculate coefficient of correlation by spearman's method from the following data: 07
 Sales(Lakhs): 45 56 39 54 45 40 56 60 30 36
 Advert.Cost : 40 36 30 44 36 32 45 42 20 36
 ('000Rs.)
 Comment on the result.
- (b) Obtain Seasonal fluctuations from the following data using moving average method: 07
 Quarterly output ('000Tons) of Commodity
 Year I II III IV
 1984 65 58 56 61
 1985 68 63 63 67
 1986 70 59 56 52
 1987 60 55 51 58
