

GUJARAT TECHNOLOGICAL UNIVERSITY**M. E. - SEMESTER – I • EXAMINATION – SUMMER • 2013****Subject code: 711507N****Date: 17-06-2013****Subject Name: Numerical Methods****Time: 10.30 am – 01.00 pm****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

Q.1 (a) Define following types of errors (i) Absolute and relative errors **06**

(ii) Inherent errors (iii) Round-off errors (iv) Truncation errors

(b) (i) Determine the absolute and relative errors involved if $x = 22/7$ is represented in normalised decimal form with 6 digits by (a) round-off (b) truncation. **08**

(ii) Determine the true error and true percentage relative error for each case.

(a) If the measured length of a track is approximated by 5999 cm and the true value is 6000 cm (b) If the measured length of a track is approximated by 59 cm and the true value is 60 cm.

Q.2 (a) Find one root of $\cos x - e^x = 0$ correct to two decimal places using suitable method. **07****(b)** Determine the equation to the best fitting exponential curve of the form $y = ax^2 + bx + c$ for the data given in Table: **07**

x	10	20	40	50	90
y	55	70	125	160	300

OR**(b)** Enlist and compare methods for curve fitting. **07****Q.3 (a)** Write a C++ programme for method of group averages of curve fitting. **07****(b)** Construct the divided difference table for data **07**

x	0.5	1.5	3.0	5.0	6.5	8.0
f(x)	1.625	5.875	31.0	131.0	282.125	521.0

Find the value of f(6)

OR**Q.3 (a)** Derive the trapezium and mid-ordinate rule for numerical integration. **07****(b)** Determine the numerical value of integration of $\log_{10}x$ for limit 1 to 2, using three-point Gauss-Quadrature rule **07****Q.4 (a)** Using the finite difference method, compute the deflection at L/4 interval of a simply supported beam subjected to central point load and full span UDL. Take EI constant. **07****(b)** Analyse a simply supported uniform square plate for uniformly distributed load by finite difference method. Take grid step L/4 in both directions. **07**

OR

- Q.4 (a)** Explain the procedure to analyse plate using finite difference method. **07**
Q.4 (b) Calculate support reactions for a prismatic fixed beam subjected to two point loads spaced at $1/3$ span, using finite difference method. **07**

- Q.5 (a)** Apply the Euler's method to the ordinary differential equation, $dy/dx = x+y$, $y(0) = 1$, using increments of size $h = 0.1$. The exact solution is $y = e^{x^2/2} - 1$. Determine the error and the percentage error at each step. **07**
(b) Determine the largest eigen value and corresponding eigenvector of the matrix $A = \begin{bmatrix} 1 & 1 & 1 \\ 2 & 1 & 2 \\ 1 & 3 & 2 \end{bmatrix}$ **07**

OR

- Q.5 (a)** Solve the following equations by Gauss Jordan method: **07**
 $x + y + z = 1$
 $4x + 3y - z = 6$
 $3x + 5y + 3z = 4$
(b) Write C++ program for any method for solution of linear simultaneous algebraic equations, except asked above. **07**
