

GUJARAT TECHNOLOGICAL UNIVERSITY**M. E. - SEMESTER – I • EXAMINATION – SUMMER • 2013****Subject code: 714702****Date: 04-06-2013****Subject Name: Advanced Control System****Time: 10.30 am – 01.00 pm****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1 (a)** Consider a Unity-feedback type-1 system with open loop transfer function **07**

$$G(s) = \frac{k}{s(s+2)}$$

It is desired to designed a cascade lead compensator such that the dominant closed-loop poles provide a damping ratio $\xi = 0.5$ and have undamped natural frequency $\omega_n = 4 \text{ rad/s}$.

- (b)** Explain the design step for the cascade lag compensator. **07**

- Q.2 (a)** The Uncompensated system transfer function is given by **07**

$$G(s) = \frac{k}{s(s+2)}$$

The system is to be compensated to meet the following specification.

Damping ratio, $\xi = 0.707$

Settling Time, $t_s \leq 5 \text{ sec}$

Velocity error constant, $k_v \geq 4$

Design a suitable lag compensator for the desired specification

- (b)** Consider a plant with transfer function **07**

$$G(s) = \frac{4}{s(s+0.5)}$$

Design a suitable lead-lag compensator to meet the following specification:

Damping ratio of dominant closed loop poles, $\xi = 0.5$

Undamped natural frequency of dominant closed loop poles, $\omega_n = 5 \text{ rad/s}$.

Velocity error constant = 80 sec^{-1} .

OR

- (b)** Consider a unity-feedback control system with open-loop transfer function **07**

$$G(s) = \frac{k}{s^2(0.2s+1)}$$

The system is required to compensate to meet the following specification.

Acceleration error constant $K_a = 10$.

Phase Margine $\geq 35^\circ$

Design a suitable lead compensator for the system.

- Q.3 (a)** Derive the solution of state equation by Laplace transform method. **07**

- (b)** Derive the model conversion from state space to transfer function. **07**

OR

- Q.3 (a)** Obtain the time response of the system given below: **07**

$$A = \begin{pmatrix} 0 & 1 \\ -2 & 0 \end{pmatrix}; \text{given } x(0) = \begin{bmatrix} 1 \\ 1 \end{bmatrix};$$

$$Y = [1 \ -1] \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

- (b)** Explain the properties of state transition matrix. **07**

- Q.4 (a)** Explain the stability analysis of sampled-data control system and mapping from s-plane to z-plane **07**

- (b)** Describe the following common nonlinear system behaviors: **07**
1. Limit cycle 2. Jump response.

OR

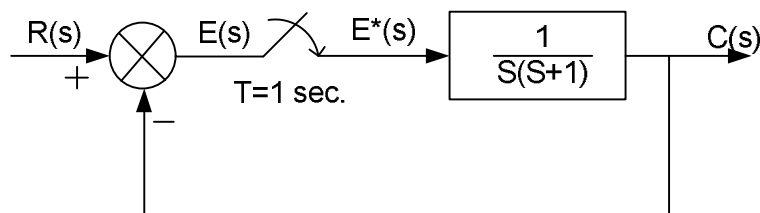
- Q.4 (a)** Describe the isoclines method of construction of phase portraits. Illustrate through an example. **07**

- (b)** Define the definition of z-transform and find the z transform of the following function: **07**

$$f(t) = e^{-at} \cos wt$$

$$f(t) = \sin wt$$

- Q.5 (a)** Find the pulse transfer function for the error sampled system shown in fig. **07**



- (b)** Draw and explain the block diagram of a control scheme employing the pole placement technique using state feedback controller. **07**

OR

- Q.5 (a)** Describe the common nonlinearities in control system. **07**

- (b)** What are singular points on phase plane? Describe the behavior of trajectory in the vicinity of commonly found singular points in phase portraits. **07**
