

GUJARAT TECHNOLOGICAL UNIVERSITY**M. E. - SEMESTER – II • EXAMINATION – SUMMER • 2014****Subject code: 1722905****Date: 20-06-2014****Subject Name: Optimization Techniques****Time: 02:30 pm - 05:00 pm****Total Marks: 70****Instructions:**

1. Attempt all questions.
2. Make suitable assumptions wherever necessary.
3. Figures to the right indicate full marks.

- Q.1** (a) Discuss scope of optimization? Give detailed classification of optimization problems. **07**
- (b) For each of the following functions : (i) $f(x) = 3x^2$ (ii) $f(x) = -5x^2$ (iii) $f(x) = 2x^2 - x^3$. Determine if $f(x)$ is convex, concave, strictly convex, strictly concave, all or none of these classes in the range $-\infty < x < \infty$. **07**
- Q.2** (a) Build a simplex table and describe its components. **07**
- (b) State necessary and sufficient conditions for stationary points. **07**
Sketch $y = x^2 - 4x$ and find stationary points.
- OR**
- (b) Bracket the minimum function $f(x) = x^2 + 54/x$ in the interval (0,5) **07**
- Q.3** (a) Solve the NLPP $\text{Max } z = 4x_1 - x_1^2 + 8x_2 - x_2^2$ **07**
subject to $x_1 + x_2 = 2$
 $x_1, x_2 \geq 0$.
- (b) Discuss three different types of optimality criteria. **07**
- OR**
- Q.3** (a) Differentiate the simplex solution procedure for a maximization and minimization problem of LPP. **07**
- (b) State advantages of duality. Obtain dual of following LPP; $\text{Min } Z = x_1 - 3x_2 - 2x_3$ **07**
Subject to the constraints,
 $3x_1 - x_2 + 2x_3 \leq 7$
 $2x_1 - 4x_2 \leq 12$
 $-4x_1 + 3x_2 + 8x_3 = 10$
- Q.4** (a) Use Lagrange multipliers to optimize $\text{Min } Z = 4x_1^2 + 5x_2^2$ **07**
Subject to the constraints, $2x_1 + 3x_2 - 6 = 0$.
- (b) Discuss Box method's algorithm to obtain optimal solution. **07**
- OR**
- Q.4** (a) Why stochastic programming is required? Explain stochastic programming with a suitable example. **07**
- (b) Penalty method transforms a constrained problem into a sequence of unconstrained problems. Justify the statement. **07**
- Q.5** (a) Why are engineers interested in optimization? State procedure for solving optimization problems. **07**
- (b) Discuss Quadratic Programming for NLP. **07**
- OR**
- Q.5** (a) State steps for GRG algorithms for unconstrained situation. **07**
- (b) Discuss a case study in dynamic programming. **07**
